

CUMULATIVE PION PRODUCTION VIA SUCCESSIVE COLLISIONS IN NUCLEAR MEDIUM *

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Production of pions in proton-nucleus (p+A) reactions outside of a kinematical boundary of proton-nucleon collisions, the so-called cumulative effect, is studied. The kinematical restrictions on pions emitted in backward direction in the target rest frame are analyzed. It is shown that cumulative pion production requires a presence of massive baryonic resonances that are produced during successive collisions of projectile with nuclear nucleons. After each successive collision the mass of created resonance may increase and, simultaneously, its longitudinal velocity decreases. Simulations within Ultra relativistic Quantum Molecular Dynamics model reveals that successive collisions of baryonic resonances with nuclear nucleons plays the dominant role in cumulative pion production in p+A reactions.

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1. Introduction

Cumulative effect in proton-nucleus (p+A) reactions is a production of secondary particles in a kinematic region forbidden in proton-nucleon (p+N) collisions at the same energy of projectile protons. First experiments with detection of cumulative particles were performed at Synchrophasotron accelerator of the Joint Institute for Nuclear Research in Dubna [1, 2, 3]. In this work inclusive reactions $p+A \rightarrow \pi(180^\circ) + X$ are considered with pions emitted in backward direction, i.e. at 180° , in the target rest frame.

Let E_π^* denotes the maximal possible energy of the pion emitted at angle 180° in the laboratory frame in p+N interaction at fixed projectile proton momentum p_0 . In p+A collisions at the same projectile proton momentum

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p_0 , pions emitted at 180° in the the nucleus rest frame with energies $E_\pi > E_\pi^*$, even above $2E_\pi^*$, were experimentally observed [1, 2, 3, 4, 5].

The main physical quantities in our analysis are the masses and longitudinal (i.e. along the collision axis) velocities of the baryonic resonances created in p+A reactions. Resonance R is first produced in $p+N \rightarrow R+N$ reaction, and it then participates in successive $R+N \rightarrow R'+N$ collisions. Due to subsequent collisions of the resonances with nuclear nucleons the resonance mass may increase and its longitudinal velocity decreases. We argue that the cumulative pions in p+A reactions are created by baryonic resonances with very high masses that are formed due to successive collisions with nuclear nucleons. We also use the UrQMD model to analyze some microscopic aspects of cumulative pion production in p+A reactions.

2. Successive collisions with nuclear nucleons

The different theoretical models were proposed to describe the cumulative pion production. However, origin of this effect is still not settled. In the present study we will advocate the approach suggested in Ref. [6]. More details are presented in our recent paper [7], where the references to other theoretical models can be also found. We assume that cumulative particle production takes place due to the large mass of the projectile baryonic resonance created in the *first* p+N collision and its further propagation through the nucleus. This baryonic resonance has a chance to interact with other nuclear nucleons earlier than it decays to free final hadrons. It can be shown [7] that during *successive collisions* of the baryonic resonance with nuclear nucleons it is possible both to enlarge the resonance mass M_R and, simultaneously, to reduce its longitudinal velocity v_R .

Production of any additional hadron(s) and/or a presence of non-zero transverse momenta in the final state would require an additional energy and lead to a reduction of E_π^{\max} value at fixed projectile momentum p_0 . Thus, to find the maximum of pion energy one should restrict the kinematical analysis to the one-dimensional (longitudinal) direction, i.e., all particle momenta should be directed along the collision axis.

If one consider baryonic resonance decay, $R \rightarrow N + \pi(180^\circ)$, the value of E_π depends on the resonance mass M_R and its longitudinal velocity v_R . In the resonance rest frame the pion energy and momentum can be easily found

$$E_\pi^0 = \frac{M_R^2 - m_N^2 + m_\pi^2}{2M_R}, \quad p_\pi^0 = \sqrt{(E_\pi^0)^2 - m_\pi^2}. \quad (1)$$

The energy E_π (with neglected pion mass for simplicity), in the laboratory

frame, is obtained as

$$E_\pi = \frac{E_\pi^0 - v_R p_\pi^0}{\sqrt{1 - v_R^2}}. \quad (2)$$

Therefore, both the increase of M_R and decrease of v_R provide an extension of the available kinematic region of E_π for pions emitted at 180° . Thus, the suppression of E_π compared to E_π^0 can be interpreted as Doppler (“red shift”) effect.

As seen from Eq. (2), both effects of resonance mass increase and its velocity decrease lead to larger values of E_π and, thus, extend the kinematic region for cumulative pion production. The object responsible for the cumulative production of $\pi(180^\circ)$, i.e., the heavy and slow moving resonance, does not exist inside a nucleus but is formed during the whole evolution process of p+A reaction.

Let us consider successive collisions with nuclear nucleons: $p+N \rightarrow R_1+N$, $R_1+N \rightarrow R_2+N$, ..., $R_n+N \rightarrow N+N+\pi(180^\circ)$. The nuclear nucleons are considered as free particles. This approximation can be justified by the fact that the projectile proton energy is typically 3 orders of magnitude larger than the binding energy of nucleons in a nucleus. It is assumed that after n -th collision the baryonic resonance decays, $R_n \rightarrow \pi(180^\circ) + N$. The energy and momentum conservation between initial and final state read as

$$\sqrt{m_N^2 + p_0^2} + n \cdot m_N = \sum_{i=1}^{n+1} \sqrt{m_N^2 + p_i^2} + E_\pi, \quad p_0 = \sum_{i=1}^{n+1} p_i - p_\pi. \quad (3)$$

The maximal pion energy E_π after n successive collisions denoted now $E_{\pi,n}^*$ can be found from Eq. (3) using the extremum conditions $\partial E_\pi / \partial p_i = 0$. This leads to

$$p_{N,n}^* \equiv p_1 = p_2 = \dots = p_{n+1} = \frac{p_0 + p_{\pi,n}^*}{n+1}, \quad (4)$$

and gives an implicit equation for $E_{\pi,n}^*$.

The maximal energies $E_{\pi,n}^*$ of pions emitted at 180° are presented in Fig. 1. A surprising behavior with $v_n^* < 0$ for $n \geq 4$ is observed at some finite regions of projectile momentum p_0 , i.e., heavy resonance may start to move backward after a large number of successive collisions for not too large p_0 . In $p+N \rightarrow R+N$ reactions the only v_R values with $v_R > 0$ are permitted.

It should be noted that the values of E_n^* and v_n^* found in this section are by no means typical (or average) ones. In fact, the probability to reach these values in p+A reaction is very small. In other words, cumulative pion production is a very rare process.

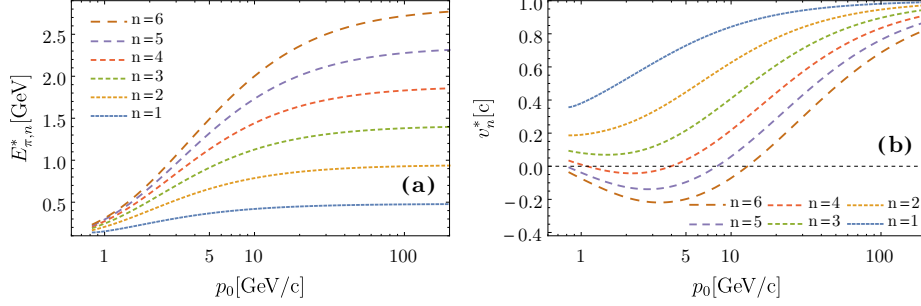


Fig. 1. Maximal energies $E_{\pi,n}^*$ (a) and velocities v_n^* (b) of the baryonic resonances after n successive collisions with nuclear nucleons. The values of v_n^* are required to provide the maximal energy $E_{\pi,n}^*$ of $\pi(180^\circ)$. They are calculated from Eq. 3 with assumption of $\partial E_\pi / \partial p_i = 0$, as functions of projectile proton momentum p_0 .

3. UrQMD simulations

In this section the analysis of the cumulative production of $\pi(180^\circ)$ within the UrQMD model [8] is presented. The UrQMD gives a unique opportunity to study a history of each individual reaction. In Fig. 2 we

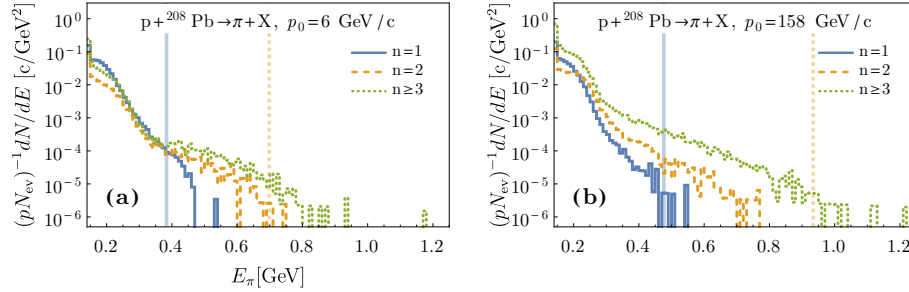


Fig. 2. UrQMD results for the pion energy spectra at 180° in $p + ^{208}\text{Pb}$ collisions. Spectra for pions created after different number of collisions with nuclear nucleons: $n = 1$ (solid line), $n = 2$ (dashed line), and $n \geq 3$ (dotted line). Vertical lines correspond to energies $E_{\pi,1}^*$ (solid) and $E_{\pi,2}^*$ (dashed). In (a) $p_0 = 6$ GeV/c and the number of events $N_{ev} = 5.7 \cdot 10^7$. In (b) $p_0 = 158$ GeV/c, $N_{ev} = 4.2 \cdot 10^7$.

compare the spectra of $\pi(180^\circ)$ emitted from resonance decay after $n = 1$ (solid line), $n = 2$ (dashed line), and $n \geq 3$ (dotted line) successive collisions of the projectile with nuclear nucleons.

From Fig. 2 one observes that E_π may exceed $E_{\pi,1}^*$ even for $n = 1$ contribution. This happens because of nucleon motion inside nuclei (Fermi motion) which exists in the UrQMD model. This effect is, however, not

large. The main contribution to the kinematical region forbidden for p+N collisions (i.e., to $E_\pi > E_{\pi,1}^*$) comes from the decays of resonances created within $n = 2$ and $n \geq 3$ successive collisions with nuclear nucleons. Therefore, the proposed mechanism of the cumulative pion production – the successive interactions of heavy resonances with nuclear nucleons – is supported by the UrQMD analysis.

4. Summary

Pions emitted in p+A reactions at 180° in the target rest frame are considered. Extension of a kinematical boundary of p+N reactions due to existence of massive baryonic resonances is studied. These resonances are produced after several successive collisions of projectile with nuclear nucleons: resonances R created in p+N reactions may have further inelastic collisions in the nuclear medium. Due to successive collisions with nuclear nucleons the masses of these resonances may increase and simultaneously their longitudinal velocities decrease. These two effects give an explanation of the cumulative pion production. The simulations of p+A reactions within the UrQMD model support this physical picture.

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